Laminar to Turbulent Transition due to unsteady Inflow Conditions:
Wind Tunnel Experiments at increased Turbulence Levels

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Abstract
Within the Luftfahrtforschungsprogramm (LuFo), measurements on a laminar flow airfoil in flight as well as in a wind tunnel are combined with direct numerical simulations (DNS) to provide the base for future improvements of transition prediction under unsteady inflow conditions.

Two regions of turbulent length scales of the inflow are of particular interest for investigating the effect on boundary layer transition on straight wings: large length scales leading to unsteady pressure distributions of the airfoil and small length scales corresponding to the streamwise wave lengths of Tollmien-Schlichting (TS) waves in the boundary layer. The current paper focuses on wind tunnel measurements of the effect of small scale turbulence.

In the Laminar Wind Tunnel of the IAG, small scale turbulence is investigated using an active grid in the settling chamber, enabling measurements at turbulence levels (Tu) ranging from 0.01% (15-5000 Hz) without grid up to 0.11%. The turbulence spectra compare very well with flight measurements in the frequency range relevant for TS-instability. Hot-wire anemometry is used for detailed boundary layer measurement while modified piezoresistive pressure transducers are utilized to measure surface pressures fluctuations up to 8 kHz.

In the range 0.01% ≤ Tu ≤ 0.11% the transition location on the pressure side of the MW-166-39-44-43 airfoil shifts upstream with increasing Tu, the frequency of the most amplified TS waves increases and the transition process change gradually from a quasi-uniform nature to a structure with isolated wave packets. Simultaneously the frequency wavenumber spectrum indicates an increased amount of energy at higher spanwise wave numbers.

The Tu dependent n-factor of the MW-166-39-44-43 airfoil was found to match very well with the modified e9 method of Mack, while the corresponding n-factor of a XIS40mod airfoil showed a much lower sensitivity, and a close to linear dependency on Tu. A variation in contribution of the receptivity coefficient in the modified e9 method did not capture the difference in Tu-dependency observed for the two airfoils.

1. Introduction
The reduction of aerodynamic friction drag through extended laminar boundary layer flow enables significant increases in the efficiency of aircraft and wind turbines. Natural laminar flow airfoils are designed to exploit this path. The most commonly used design methodologies (Croach 2015) rely on the prediction of boundary layer transition based on the e9 method, which typically assumes steady boundary conditions. However, airfoils of aircraft and wind turbines are exposed to atmospheric turbulence which results in unsteady inflow conditions.

The spectrum and intensity of atmospheric turbulence has been investigated from various perspectives. For example Shei et al. 1971 measured a very large range of length scales utilizing an aircraft and a meteorology mast, Li et al. 2014 published measurements in low wind conditions as well as strong winds (typhoon), Chougule and Mann 2015 investigated the difference between the turbulence over open terrain and forest and Bodini et al. 2018 used LiDAR to map the turbulence from the ground up to several hundred meters. The results fit well with a spectrum based on the Kolmogorov hypotheses (Kolmogorov 1941) with its three distinct regions: the energy containing range, the inertial subrange and the dissipation subrange (Pope 2000).

Flight measurements of the inflow conditions were performed by Otten et al. 1982 at an altitude ranging from 3.7 km to 12 km. They found very low turbulence levels in the order of 0.02%. Zarnin 1984 was probably the first to measure the atmospheric turbulence level with a glider at altitudes below 1200 m. The reported turbulence intensities varied around 0.2% (1-5000 Hz), much higher than Otten et al.

Nitsche et al. 2001, Peltzer 2004 and Seitz and Horstmann 2006 have investigated the transition from laminar to turbulent boundary layer in flight conditions, mainly focusing on low turbulence conditions, i.e. Tu = u’/Uinf ≤ 0.05%.

Reeh 2014 performed flight measurements on a natural laminar flow airfoil at different levels of atmospheric turbulence. He proposed to separate the effect of the freestream turbulence into large scale and small scale turbulence. The large scale causes unsteady variations in the inflow angle, which in turn results in unsteady variations of the pressure distribution to which the boundary layer responds. The small scale turbulence enters the boundary layer through receptivity (Morkovin 1977) and provides initial amplitudes of disturbances within the boundary layer.

Field measurements of the transition on wind turbines are less frequent in the literature. Madsen et al. 2010 used surface mounted microphones on an 80 m diameter rotor in the DAN-AERO projects and Schaffarczyk et al. 2014 performed measurements on a 33 m diameter rotor using hot films. Although less conclusive than the mentioned flight investigations, the two measurements on wind turbines show significant portions of laminar boundary layer as well as the atmospheric turbulence influencing the boundary layer transition.

Based on a huge set of wind tunnel tests Kendall 1990 found that below Tu ≤ 0.2-0.5% transition takes place through amplification of Tollmien-Schlichting (TS) waves with wave packets gradually occurring at...
increased turbulence. At higher turbulence levels the formation of streaks and low frequency disturbances (Klebanoff modes) tend to dominate the transition process and bypass transition occurs, see the review by Durbin 2017. The upper level of turbulence for which the TS-type transition is dominating is not clear from the literature. Arnal and Juillen 1978 (see also Kendall by Durbin 2017. The upper level of turbulence for which Klebanoff modes tend to dominate the transition formation of streaks and low frequency disturbances levels of small scale turbulence.

The stationary base flow and the impact of increased prediction under unsteady inflow conditions. Together with results from direct natural laminar flow airfoil are performed both in flight transition with the target of improved understanding of the Luftfahrtforschungsprogramm (LuFo), is focusing on unter instationären Anströmbedingungen, supported by atmospheric turbulence (Tu up to around 0.1%).

Turbulence in the range of interest for low to moderate relevant transition mechanism for small scale transition with the target of improved understanding of the spectral energy distribution covered by the integral Tu level, this points at TS-waves being the bypass transition was prevailing. Beside the importance of the spectral energy distribution covered by the integral Tu level, this points at TS-waves being the transition scenario was dominated by unsteady streamwise streaks. Suder and O’Brian 1988 found TS-type transition at Tu = 0.3%, while at 0.65% bypass transition was prevailing. Beside the importance of the atmospheric turbulence (Tu up to around 0.1%).

The ongoing project "Laminar-turbulente Transition unter instationären Anströmbedingungen", supported by the base turbulence level in the range of interest for low to moderate atmospheric turbulence (Tu up to around 0.1%). The ongoing project "Laminar-turbulente Transition unter instationären Anströmbedingungen", supported by the Luftfahrtforschungsprogramm (LuFo), is focusing on the effects of atmospheric turbulence on boundary layer transition with the target of improved understanding of the underlying mechanisms. Measurements on a natural laminar flow airfoil are performed both in flight and in the wind tunnel. Together with results from direct numerical simulation (DNS) the measurements will provide a base for future improvements of transition prediction under unsteady inflow conditions.

This paper describes wind tunnel investigations of the stationary base flow and the impact of increased levels of small scale turbulence.

2. Measurement setup and data acquisition
2.1. Wind tunnel and airfoil models

The measurements were performed in the Laminar Wind Tunnel (LWK) of the Institute for Aerodyamics and Gas Dynamics (IAG) in Stuttgart. The wind tunnel has an open return and a closed test section with a cross section of 0.73 x 2.73 m² and a length of 3.15 m. The base turbulence level is very low due to the high contraction ratio (effectively 20:1) and the use of several screens and filters in the inlet part of the tunnel. At 38 m/s the base turbulence level is 0.01% in the range 15-5000 Hz. The background noise level is kept low through sound absorbing lining in the first part of the tunnel.

The model is equipped with 42 pressure taps with 0.4 mm diameter which are distributed from x/c = 0.01 on the suction side to x/c = 0.73 on the pressure side. The taps upstream of x/c = 0.05 are offset 20° in spanwise direction to minimize disturbance between taps. A spanwise row of 14 pressure taps with 7 mm spacing is located at x/c = 0.311. At each end of the row a flush mounted Kulite XCQ-062-5D is used as reference pressure transducer.

A small influence on the transition was produced by the pressure taps upstream x/c = 0.15 and for most of the measurements these taps were closed by a 40 μm thick and 12 mm wide adhesive tape. For the transition detection measurements with IR thermography those taps were sealed with gelcoat and the surface sanded smooth.

A universal disturbance source is located at x/c = 0.15. The disturbance source was not used in the current measurements and was sealed by a 40 μm thick and 12 mm wide adhesive tape for most of the measurements. For the transition detection measurements with IR thermography the slit was sealed with an elastic polyurethane compound (Teroson PU-92) which was sanded to match the airfoil contour.

Additional measurements were performed on a 0.6 m chord XIS40mod airfoil model which is of similar construction as the MW-166-39-44-43. The XIS40mod is a symmetric, 15% maximum thickness airfoil designed for transition investigations, see Würz 1995 for details.

2.2. Data acquisition and processing

Three main measurement techniques have been used for the present investigations: surface pressures (both steady and unsteady), hot-wire anemometry (in the boundary layer or the freestream) and infrared thermography.

Steady surface pressures were measured at all pressure taps by a PSI ESP64HD pressure scanning module.

Unsteady surface pressures were measured at every second pressure tap using discrete piezoresistive transducers (SensorTechnics HCL0050T) which have been modified to reduce the internal volume and to allow an installation similar to Franzoni and Elliott 1998 and Perennes and Roger 1998, using the 2.0 m long tube to the PSI pressure scanner as damping pipe. This effectively connects the discrete HCL transducer and PSI unit in parallel, allowing measurements with both systems simultaneously. The transducer modifications, the special installation and a frequency dependent calibration enable measurements of unsteady pressures up to 8 kHz.

The signals from the HCL transducers were split in a DC part and an AC part and amplified by low noise amplifiers (Cosytec BRVST2).

Boundary layer hot-wire measurements have been conducted with a DANTEC 55P15 single hot-wire probe with a 5 μm wire controlled by a DISA 55M10 constant temperature anemometer (CTA). The probe was positioned using a computer controlled traversing unit with a traversing accuracy of 5 μm in wall normal direction and 100 μm in spanwise direction.

The hot-wire signal was divided in a DC component and an AC part where the AC part was high pass filtered at 50 Hz and amplified depending on the signal level by an AMI 351A-1-50-NI amplifiers.

The signals from both the unsteady surface pressure transducers and the boundary layer hot-wire were acquired using an 80 channel, 16 bit NI USB-6255 AD-converter sampling at 15650 Hz. Low pass filters with 4.8 kHz corner frequency were used for anti-aliasing.

The freestream turbulence was measured using a separate measurement system consisting of a straight
hot-wire probe with a 2.5 μm diameter wire, a DISA 55M10 CTA anemometer, an AMI 321A-3-50-NI amplifier and a low pass filter with corner frequency of 15 kHz for signal conditioning. The signal was acquired using the 24 bit Sigma-Delta ADC inputs of a RME Hammerfall Multiface DSP sampling at 44.1 kHz.

A FLIR X6540sc IR camera was used to determine the transition location. The maximum of the temperature gradient in streamwise direction was used to define the transition location.

For the comparison of the experimental results with linear stability theory (LST) a three step procedure was used: i) viscous pressure distributions were calculated by XFOIL V6.96, ii) Based on these distributions the boundary layer parameters were determined using a finite differential scheme (Cebeci and Smith 1974) and iii) the Orr-Sommerfeld equation was addressed with a shooting solver (Conte 1966).

2.3. Turbulence generation

Small scale turbulence is generated by an active, pneumatic grid according to the method described by Kendall 1990 where the grid is placed in the settling chamber of the wind tunnel. The 2 m by 2 m grid consists of 2 mm horizontal tubes with 0.2 mm diameter holes which generate tiny jets blowing upstream as compressed air is applied through the tubes of the grid. The pressure level of the supplied air controls the resulting turbulence level in the test section. At $u_{ref} = 38$ m/s a turbulence level between 0.03% and 0.11% can be set ($Tu = 0.01\%$ without grid).

Figure 1 shows the freestream turbulence spectrum wind tunnel (with and without active grid), in flight and model spectrum.

Figure 1 shows the frequency spectrum of the freestream turbulence with and without the grid. Compared to flight measurements and a model spectrum according to Pope 2000 the wind tunnel spectrum captures the dissipative subrange above 400 Hz very well. Toward lower frequencies the flight measurements show a clear inertial subrange with the familiar -5/3 exponent slope. In this range the slope of the spectrum from the wind tunnel is less steep and the two spectra gradually diverge below 400 Hz. In the current experiment Tollmien-Schlichting amplification occurs in a range of frequencies $300 \leq f \leq 2000$ Hz in which the inflow measurement in the atmosphere and the wind tunnel matches well.

3. Results and discussion

3.1. Base flow - low turbulence level ($Tu = 0.01\%$)

A reference case of $\alpha = -1.4^\circ$ and Re = $3.4 \cdot 10^6$ has been selected based on the measured conditions for cruise/dash flight close to the lower corner of the laminar bucket of the airfoil. All measurements are made on the pressure side of the airfoil which is the most sensitive side for the selected reference condition.

To compensate for the influence of the wind tunnel walls, the angle of attack of the wind tunnel model has been adjusted to match the measured pressure gradient with a RANS calculation of the simulated flight condition in the range $0.05 < x/c < 0.4$. As can be seen in figure 2 an offset remains in the pressure distribution although this is not regarded as important for the boundary layer development. Hereafter $\alpha_{ref}$ will be used for -1.4° angle of attack in free flight and simulations as well as for -0.7° geometric angle of attack in the wind tunnel.

Figure 2. Pressure distribution from measurement and RANS simulation.

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Figure 3 shows the measured mean boundary layer parameters compared with DNS. The measured
displacement thickness $\delta_1$ and shape factor $H_{12}$ lies slightly below the simulations while the momentum thickness $\delta_2$ matches very well. The drop in $H_{12}$ at transition occurs earlier in the experiment than in the simulations.

Figure 4. Measured boundary layer velocity profiles. The profile at $x/c = 0.166$ is compared with DNS (both shifted by 0.2 to the right for clarity).

The normalized boundary layer profiles from $x/c = 0.166$ through $x/c = 0.337$ in figure 4 show a close similarity which is to be expected from the near constant shape factor $H_{12}$ and the match with DNS results is good.

The hot-wire traversing unit and the adhesive tape over the universal disturbance and pressure taps upstream of $x/c = 0.15$ had an effect on the transition which explains the shift in transition location between the measurements with hot-wire, unsteady surface pressures (without hot-wire traversing unit) and IR thermography (no hot-wire traversing unit or tapes). Since the measured amplification rates with both the hot-wire traversing unit and tape over the disturbance

source present (figure 5) match well with linear stability theory and the DNS results it is assumed that the influence can be regarded as an increase of the initial disturbance level $A_0$ due to local receptivity and that the stability characteristics of the boundary layer remains the same as without hot-wire traverse unit and the tapes.

Figure 5. Comparison of measured amplification rates to LST and DNS.

In figure 6 the measured eigenfunction at $x/c = 0.262$ and $f = 908$ Hz is compared to DNS results for a 2D wave. Since the experimental eigenfunction is a composition of 2D and 3D waves, differences are visible close to the second wall near maximum.

Figure 6. Eigenfunctions from measurement and DNS. $x/c = 0.262$, $\alpha_{eq}$, $f = 908$ Hz, 2D waves used in simulation.

The downstream evolution of spectra from the unsteady surface pressures (figure 7) show a first Tollmien-Schlichting "hump" with a centre frequency of about 1000 Hz visible above the electric noise floor at $x/c = 0.286$. TS frequencies are further amplified downstream with a shift to lower frequencies. At $x/c = 0.396$ higher harmonics continuous appear and at $x/c = 0.464$ strong non-linear effects are seen with a fill-up of the spectrum at frequencies both below and above the most amplified frequencies. Downstream $x/c = 0.540$ the typical spectrum of a turbulent boundary layer emerges.

Figure 7. Spectra of unsteady surface pressures compared with 2D LST for $x/c = 0.396$.

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A direct comparison with linear stability theory is difficult due to the mixture of 2D and 3D waves, but a coarse comparison of spectra at $x/c = 0.396$ show a very good agreement in frequency range. The LST spectrum is based on a flat $A_0$ distribution with an initial...
amplitude adjusted to match the peak amplitudes of the LST and the experiment.

The wall normal spectra (figure 8) show a linear stage at positions x/c = 0.262 and 0.311 with amplification of TS-modes and typical TS-wave eigenfunctions. At x/c = 0.337 a non-linear stage can be seen with the above described fill-up of the spectrum at frequencies outside the TS-region. This is as expected in a classic TS-wave transition at low turbulence levels and a moderate adverse pressure gradient.

The spanwise wave number spectra of the unsteady surface pressures at x/c = 0.311 and υ/υ' ref (figure 9a) correspond well with the energy spectra from linear stability theory (figure 9b, spanwise wave number independence of the transfer function to surface pressure assumed) in the region of most amplified frequencies. The measurement shows lower amplitudes for larger wave numbers than the LST and some non linear mode amplification can be seen for small wave numbers around 600 Hz and 1400 Hz. The main characteristics of the wavenumber spectrum matches with the spectrum measured on the same airfoil in flight at x/c = 0.482 and υ/υ' = -0.92° (slightly earlier in the transition process) by Reeh 2014.

3.2. Effects of increased small scale turbulence
As can be seen in figure 10, an increase of the freestream turbulence level reduces the maximum TS-amplitudes and the "TS-hump" broadens. The transition location moves forward and the frequency of the TS-maximum is shifted upwards. The shift in frequency is at least partly attributed to the linear stability
characteristics as the amplification of higher frequencies is favoured at upstream positions (compare figure 7).

Comparing spanwise wavenumber spectra for different turbulence levels is somewhat difficult since the transition location moves with turbulence level and a fixed spanwise row of surface pressure taps exists. Therefore figure 11 shows approximately the same stage in the transition process at $Tu = 0.01\%$ and $0.07\%$. The angle of attack has been adjusted to position the transition in relation to the spanwise row of pressure taps ($\alpha = \alpha_{\text{ref}} - 0.2^\circ$ and $\alpha = \alpha_{\text{ref}} + 1.0^\circ$ respectively). The procedure is somewhat coarse, but an increase of amplitudes at higher spanwise wavenumbers can be seen in the case with higher freestream turbulence.

The time traces of the unsteady pressure taps in streamwise direction reveal a change in the structure of the transition process from the quasi-uniform nature at $Tu = 0.01\%$ (figure 12a) to a structure with formation of isolated wave packages which grow into turbulent spots at $Tu = 0.11\%$ (figure 12b). The change is gradual over the $0.01\% - 0.11\%$ range of turbulence in the present investigation. The forming of wave packets has been observed by Kendall 1990 when increasing the freestream turbulence from $Tu = 0.03\%$ to $Tu > 0.1\%$ and wave packets were observed in flight measurements by Seitz and Horstmann 2006 at an estimated $Tu \leq 0.05\%$.

The effect of freestream turbulence on the transition location has been measured in parallel using IR thermography and corresponding n-factors have been determined using linear stability theory. The main advantage of this non-intrusive method is the full spanwise-streamwise information which allows identifying and avoiding regions with high receptivity, e.g. pressure taps. The results are compared to the modified $e^5$ method of Mack 1997 in figure 13. It should be noted that the method of Mack is based on flat plate measurements and that the data used by Mack showed little change in critical n-factor below $Tu = 0.1\%$, an effect typically attributed to the sound component of the disturbance environment in the wind tunnel controlling the transition (Mack 1977) at low Tu. Consequently the valid range for the method is given as $Tu > 0.1\%$.

Although the current transition location measurements on the MW-166-39-44-43 have been performed in the range $0.03\% \leq Tu \leq 0.11\%$, there is a very good match with the curve of the modified $e^5$ method. In the measured range, $n_c$ changes from 11.8 to 8.1 and the gradient steepens toward lower turbulence levels. Measurements in a slightly different configuration (data not included here) indicates that the trend continues also down to $Tu = 0.01\%$. 

Figure 11. Frequency wavenumber spectra at $x/c = 0.311$. a) $Tu = 0.01\%, \alpha_{\text{ref}} - 0.2^\circ$, b) $Tu = 0.07\%, \alpha_{\text{ref}} + 1.0^\circ$

Figure 12. Time traces of surface pressures at a) $Tu = 0.01\%$ and b) $Tu = 0.11\%$. The time traces of the unsteady pressure taps in streamwise direction reveal a change in the structure of the transition process from the quasi-uniform nature at $Tu = 0.01\%$ (figure 12a) to a structure with formation of isolated wave packages which grow into turbulent spots at $Tu = 0.11\%$ (figure 12b). The change is gradual over the $0.01\% - 0.11\%$ range of turbulence in the present investigation. The forming of wave packets has been observed by Kendall 1990 when increasing the freestream turbulence from $Tu = 0.03\%$ to $Tu > 0.1\%$ and wave packets were observed in flight measurements by Seitz and Horstmann 2006 at an estimated $Tu \leq 0.05\%$.

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The good match between the current measurements at $Tu < 0.1\%$ and the modified $e^9$ method could be linked to the low level of acoustic noise in the LWK wind tunnel (72 dBA at 39 m/s, Plogmann and Würz 2013), leaving the freestream turbulence as the dominating disturbance source at lower turbulence levels than seen in the data used by Mack.

The method of Mack is essentially based on the idea of a constant receptivity factor for transformation of outer disturbances into TS-waves, a linear amplifier (LST) and an amplitude threshold at transition. When using this method on airfoils instead of flat plates, one can assume that the receptivity factor is different.

In order to investigate the influence of the receptivity coefficient on Mack’s modified $e^9$ method, a ratio between receptivity coefficients is defined as

$$ k_r = \frac{G_{\text{current}}}{G_{\text{Mack}}} $$

where $G_{\text{Mack}}$ and $G_{\text{current}}$ are the receptivity coefficients in the experiment used my Mack and in the current measurement respectively. Introducing the receptivity coefficient ratio $k_r$ into the equation of Mack yields

$$ n_{tr} = -8.43 - 2.4 \cdot \ln(k_r \cdot Tu) $$

Evaluating this expression for different $k_r$ shows that a change in the receptivity coefficient results in a vertical shift of the $n$-factor curve (figure 13). This means that a change in receptivity coefficient moves the transition similar to a change in $Tu$.

To get an impression of the applicability of the modified $e^9$ method to other base flows, IR transition location measurements have been conducted on a XIS40mod airfoil at $\alpha = 2^\circ$ and $Re = 1.5 \cdot 10^6$ (figure 14). The results show a different behaviour of the $n$-factor compared to the MW-166-39-44-43 for which the gradient increases towards smaller $Tu$.

The differences in the base flow between the two airfoils causes a significant difference in the response to freestream turbulence level. The difference manifests itself as a change in slope and curve form and is not captured by a change in the receptivity coefficient. The mechanism behind these differences has not yet been clarified.

4. Conclusions

Measurements of the boundary layer transition on the MW-166-39-44-43 natural laminar flow airfoil at unsteady inflow conditions have been performed in the Laminar Wind Tunnel at the IAG, University of Stuttgart.

As small scale turbulence is increased from 0.01\% to 0.11\% the transition location shifts upstream, the frequency of the amplified TS waves increases and the transition process changes gradually from a quasi-uniform nature to a structure with isolated wave packets. The frequency wavenumber spectrum indicates an increased amount of energy at higher spanwise wave numbers.

In the range $0.03\% \leq Tu \leq 0.11\%$ the $n$-factor of the MW-166-39-44-43 airfoil was found to match very well with the modified $e^9$ method of Mack 1997. In contrast a XIS40mod airfoil showed a much smaller change in $n$-factor, less than half compared to the MW-166-39-44-43 and with a close to linear dependency of $Tu$. The difference in response to freestream turbulence between the two airfoils is not captured by a variation of the receptivity coefficient since the contribution of the receptivity shifts the level of the $n$-factor curve but does not affect the slope of the curve.

Affiliation

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